



# **SPATIAL PHARMACOKINETIC- TOXICOKINETIC MODELLING**

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# STOCHASTIC-REACTION DIFFUSION SYSTEMS



- **The mathematical core of Redi**
- Generalized Fick's first and second laws with state dependent diffusion coefficients.
- Stochastic selection of diffusion and chemical reaction events.

## Inputs

- Molecular mass of diffusing particle
- Chemical reactions eventually involved in the system and their kinetic rates
- Initial local concentrations of the species.



# GEMCITABINE DIFFUSION AND TUMOR SHRINKAGE

The reaction-diffusion system involves two components drug (D), i.e. gemcitabine, and tumor cell (T) and the following events:

- gemcitabine diffusion (molecular weight of 299.66)
- gemcitabine degradation
- effective interaction of gemcitabine and death of tumor cell
- uneffective interaction of gemcitabine: the tumor cell survives
- tumor growth

Tumor size model:

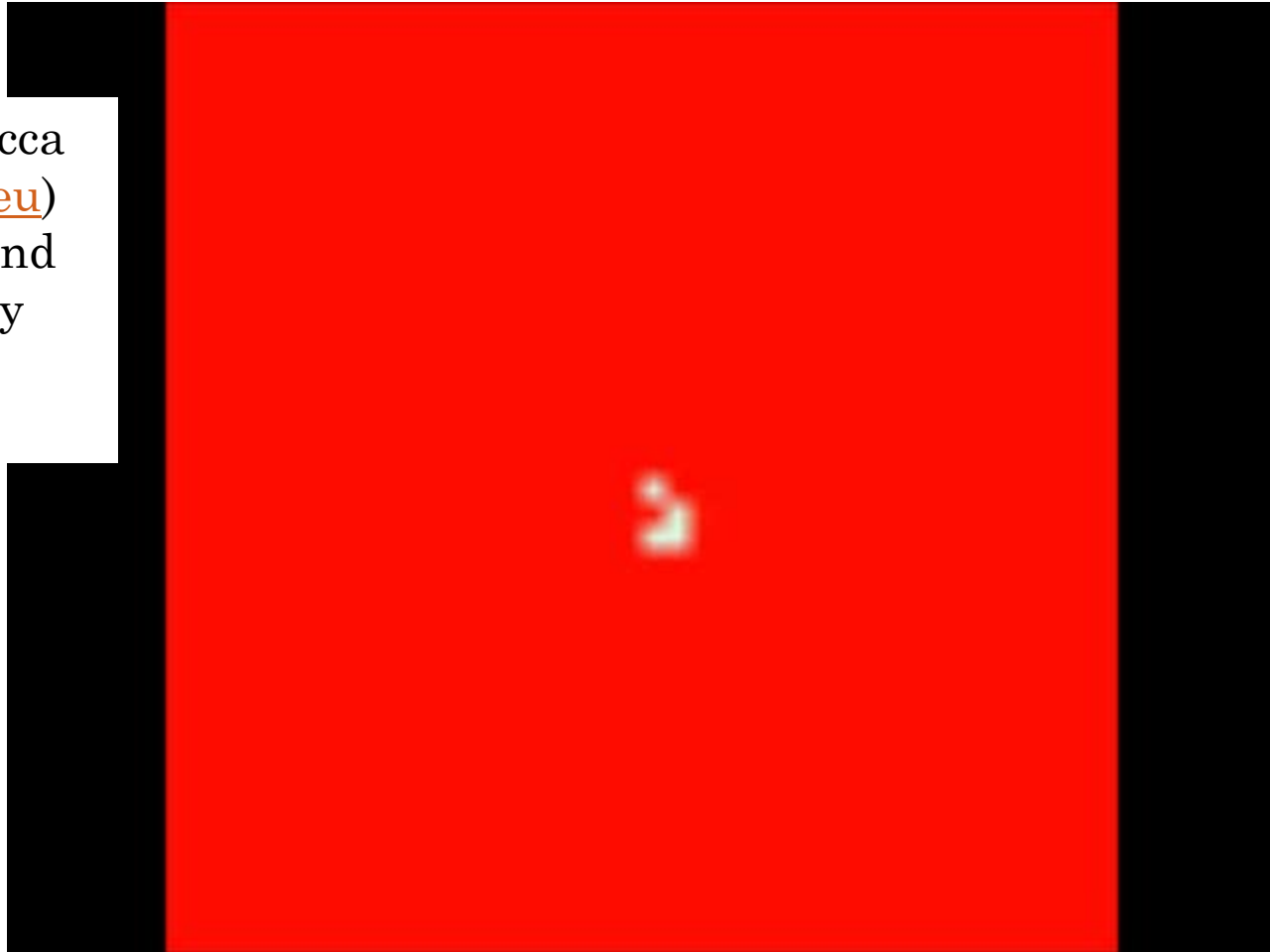
- irregular 2D spheroidal tumor of 3 mm

Interaction	Rate constants
R1 : $D \xrightarrow{k_1} \emptyset$	$k_1 = 0.1 \text{ hours}^{-1}$
R2 : $D + T \xrightarrow{k_2} \emptyset$	$k_2 = 0.0001 \text{ (cm} \cdot \text{hours)}^{-1}$
R3 : $D + T \xrightarrow{k_3} T$	$k_3 = 0.001 \text{ (cm} \cdot \text{hours)}^{-1}$
R4 : $T \xrightarrow{k_4} T + T$	$k_4 = 0.02 \text{ cm} \cdot \text{hours}^{-1}$
Category of patient	Median value of efficacy
Male	$0.03817219 \text{ (cm} \cdot \text{hours)}^{-1}$
Female	$0.03815441 \text{ (cm} \cdot \text{hours)}^{-1}$
Smoker	$0.02937583 \text{ (cm} \cdot \text{hours)}^{-1}$
Ex-smoker	$0.07753538 \text{ (cm} \cdot \text{hours)}^{-1}$
Non-Smoker	$0.03815441 \text{ (cm} \cdot \text{hours)}^{-1}$



# TIME EVOLUTION OF THE TUMOR

Refer to P. Lecca  
([lecca@cosbi.eu](mailto:lecca@cosbi.eu))  
for a longer and  
higher-quality  
video of the  
simulation.



Duration of gemcitabine treatment: 14 weeks

# REFERENCES

Redi: <http://www.cosbi.eu/index.php/research/prototypes/redi>

P. Lecca, O. Kahramanogullari, D. Morpurgo, C. Priami, R. Soo, Modelling and estimating dynamics of tumor shrinkage with BlenX and KInfer,, UKSim 2001 - 13th International Conference on Modelling and Simulation,2011

P. Lecca, L. Dematte', A. Ihekwaba, C. Priami, Redi: a simulator of stochastic biochemical reaction-diffusion systems, The Second International Conference on Advances in System Simulation (SIMUL 2010)

